Factors & Sampling

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Today's Lecture

1. A little bit about Factors
2. Sampling
3. Describing your sample

Quick Review of Last Week's Computational Concepts

1. Objects
2. Functions manipulating objects
3. Data frames
4. Vectors
5. Numeric, Character, Boolean, and Factor objects…

Numbers we Understand

```
summary(westNile$WNV.incidence)
```

```
#    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
#   -7.31    0.00    0.05    1.45    1.91   24.40
```

What is this?

```
summary(westNile$State)
```

```
# AL CT DE FL GA IL IN KY MA MD MI MS NH NJ NY OH PA TN WI WV
# 19  2  1  2  2 14  6  2  4  8  6  1  2  4  8  4 14  4 22  5
```

What is a factor?

- A factor is made up of text strings
- A factor has levels

```
westNile$State[1:10]
```

```
#  [1] AL AL AL AL AL AL AL AL AL CT
# Levels: AL CT DE FL GA IL IN KY MA MD MI MS NH NJ NY OH PA TN WI WV
```

```
levels(westNile$State)
```

```
#  [1] "AL" "CT" "DE" "FL" "GA" "IL" "IN" "KY" "MA" "MD" "MI" "MS" "NH" "NJ" "NY"
# [16] "OH" "PA" "TN" "WI" "WV"
```

Numerics, Characters, and Factors

```
#a numeric vector
c(1,2,3)
```

```
# [1] 1 2 3
```

```
#a character vector
c("1", "2", "3")
```

```
# [1] "1" "2" "3"
```

```
#a character vector -> factor
factor(c("1", "2", "3"))
```

```
# [1] 1 2 3
# Levels: 1 2 3
```

Characters v. Factors

```
as.character(westNile$State[1:10])
```

```
#  [1] "AL" "AL" "AL" "AL" "AL" "AL" "AL" "AL" "AL" "CT"
```

```
westNile$State[1:10]
```

```
#  [1] AL AL AL AL AL AL AL AL AL CT
# Levels: AL CT DE FL GA IL IN KY MA MD MI MS NH NJ NY OH PA TN WI WV
```

This is important, as *which* does not work with factors!

Exercise

- Create a factor vector of the letters A thorugh D that repeats 10 times (use rep)
- Do the same thing, but with the strings A1, B1, …D1
- Merge these two into a single vector.

Solution

```
v1<-factor( rep(c("A", "B", "C", "D"), 10))

v2<-factor( rep(c("A1", "B1", "C1", "D1"), 10))

v3<-factor(c(as.character(v1), as.character(v2)))

v3[1:20]
```

```
#  [1] A B C D A B C D A B C D A B C D A B C D
# Levels: A A1 B B1 C C1 D D1
```

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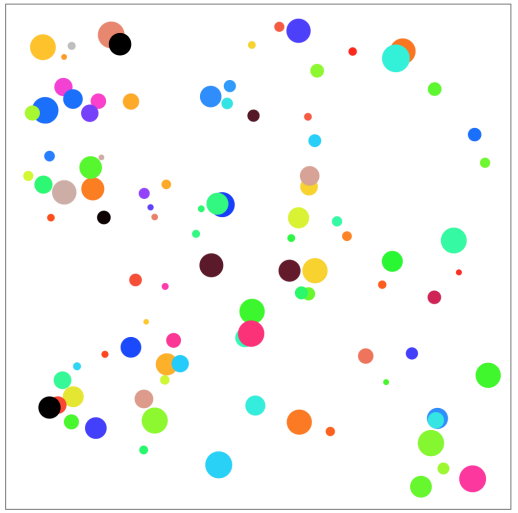
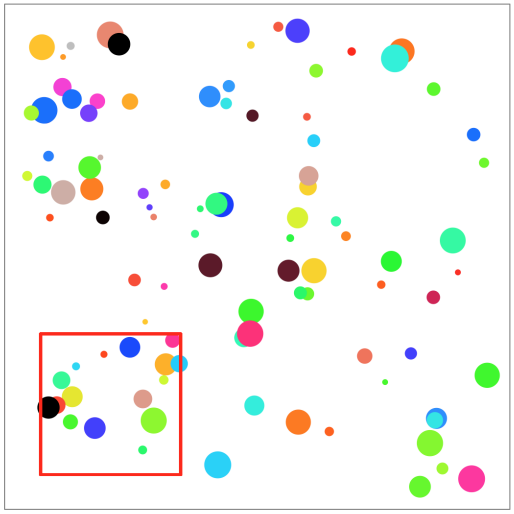
3. Describing your population

What is a population?



What is a sample?

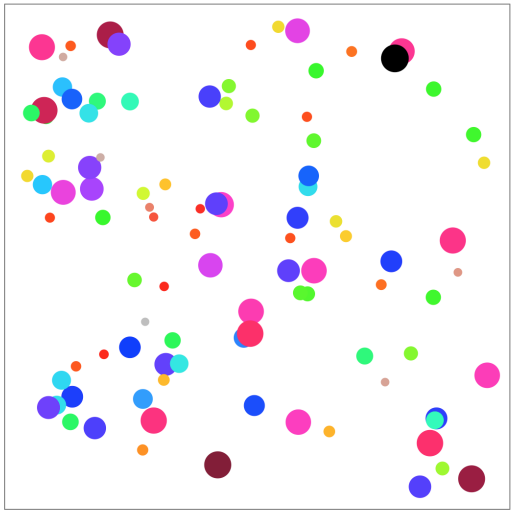


A **sample** of individuals in a randomly distributed population.

How can sampling a population go awry?

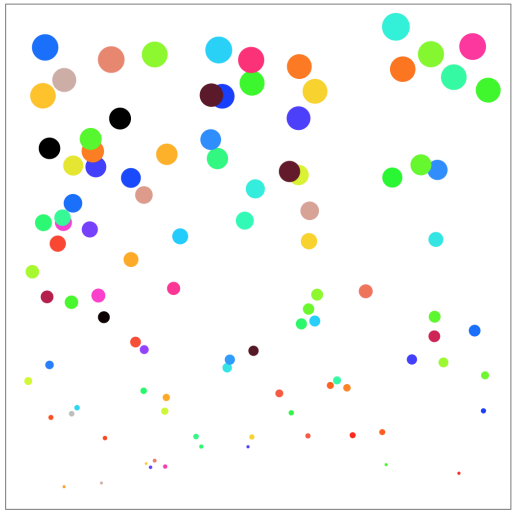
- Sample is not **representative**
- Replicates do not have **equal chance** of being sampled
- Replicates are not is not **independent**

Bias from Unequal Representation



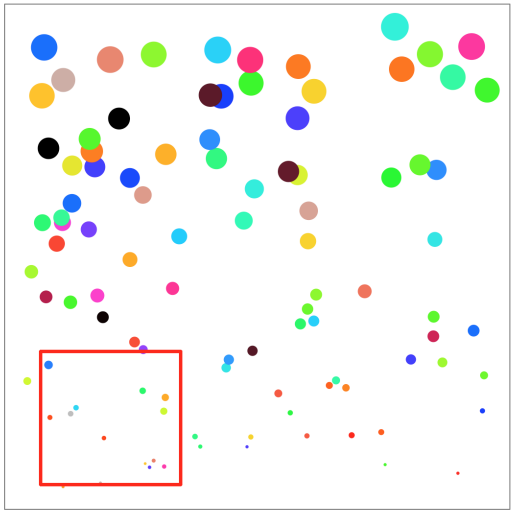
If you only chose one color, you would only get one range of sizes.

Bias from Unequal Change of Sampling



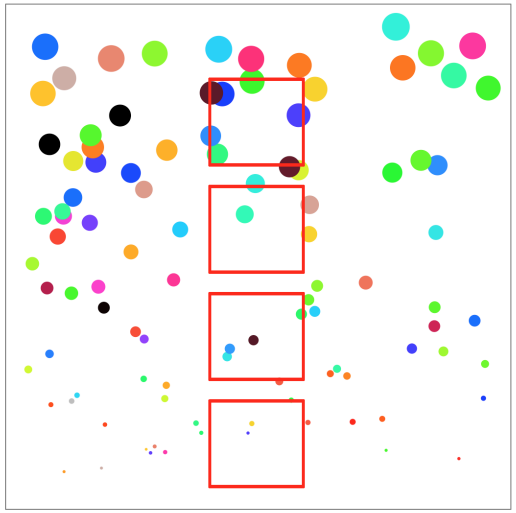
Spatial gradient in size

Bias from Unequal Change of Sampling



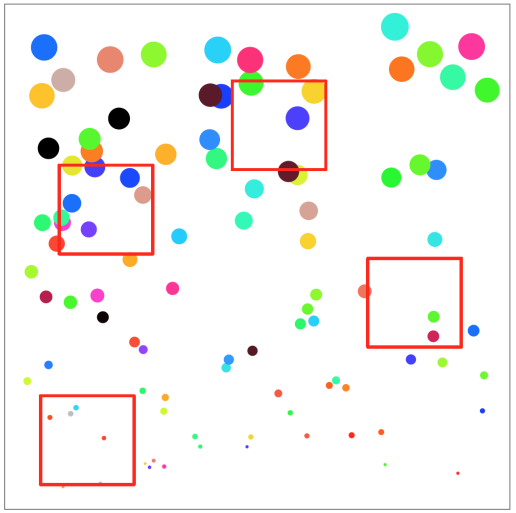
Oh, I'll just grab those individuals closest to me…

Solution: Stratified Sampling



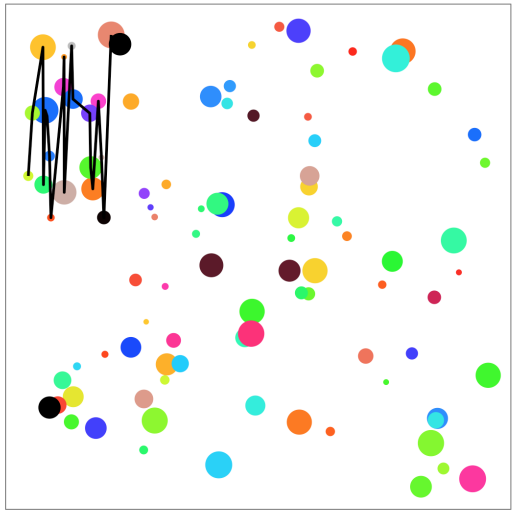
Sample over a known gradient, aka **cluster sampling**

Solution: Random Sampling



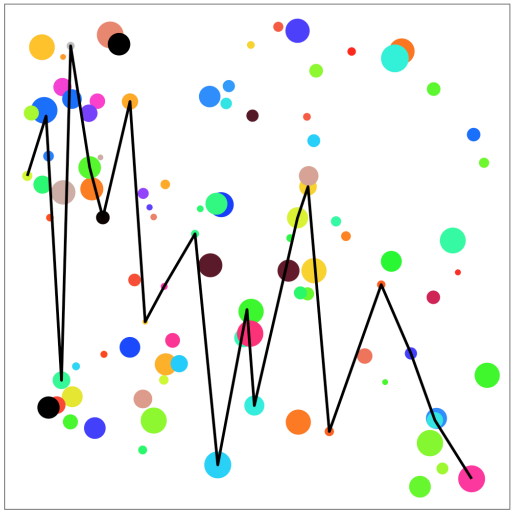
Two sampling schemes:

Non-Independence & Haphazard Sampling



What if there are interactions between individuals?

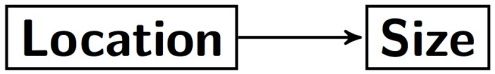
Solution: Chose Samples Randomly



Path chosen with random number generator

Deciding Sampling Design

What influences the measurement you are interested in?



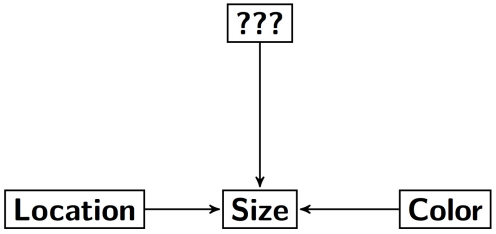
Causal Graph

Stratified or Random?

Do you know all of the influences?

Stratified or Random?

Do you know all of the influences?



You can represent this as an equation:
Size = Color + Location + ???

Stratified or Random?

- How is your population defined?
- What is the scale of your inference?
- What might influence the inclusion of a replicate?
- How important are external factors you know about?
- How important are external factors you cannot assess?

Exercise

Draw a causal graph of the influences on one thing you measure

How would you sample your population?

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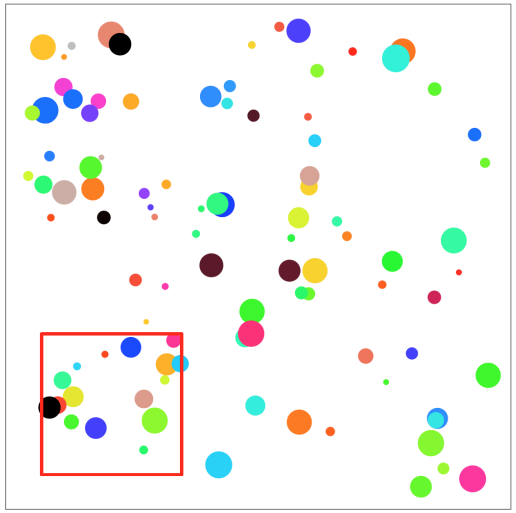
Sample Properties: Mean



Sample Properties: Mean

$$\bar{Y} = \frac{\sum_{i=1}^{n} y_i}{n}$$

$\bar{Y}$ - The average value of a sample
x_i - The value of a measurement for a single individual
n - The number of individuals in a sample

μ - The average value of a population
(Greek = population, Latin = Sample)

R: Sample Size and Estimate Precision

As n increases, does your estimate get closer to the true mean?

1. Taking a mean

```
mean(c(1,4,5,10,15))
```

```
# [1] 7
```

R: Sample Size and Estimate Precision

As n increases, does your estimate get closer to the true mean?

2. Mean from a random population

```
mean(runif(n = 500, min = 0, max = 100))
```

```
# [1] 47.53
```

runif draws from a Uniform distribution

R: Sample Size and Estimate Precision

As n increases, does your estimate get closer to the true mean?

3. Sampling from a single simulated population

```
set.seed(5000)
population<-runif(400,0,100)
mean( sample(population, size=50) )
```

```
# [1] 46.83
```

set.seed ensures that you get the same random number every time
sample draws a sample of a defined size from a vector

Exercise: Sample Size and Estimate Precision

As n increases, does your estimate get closer to the true mean?

1. Use runif (or rnorm, if you're feeling saucy) to simulate a population
2. How does the repeatability of the mean change as you change the sample size?

Exercise: Sample Size and Estimate Precision

As n increases, does your estimate get closer to the true mean?

```
set.seed(5000)
population<-runif(n = 400, min = 0, max = 100)
mean( sample(population, size=3) )
```

```
# [1] 64.52
```

```
mean( sample(population, size=3) )
```

```
# [1] 54.91
```

Exercise: Sample Size and Estimate Precision

As n increases, does your estimate get closer to the true mean?

Let's try a larger sample size and check in on repeatability…

```
mean( sample(population, size=100) )
```

```
# [1] 45.06
```

```
mean( sample(population, size=100) )
```

```
# [1] 45.96
```

Sample Properties: Variance

How variable was that population?

$$s^2 = \frac{\sum_{i=1}^{n} (Y_i - \bar{Y})^2}{n-1}$$

- **Sums of Squares** over n-1
- n-1 corrects for both sample size and sample bias
- σ^2 if describing the population
- Units in square of measurement…

Sample Properties: Standard Deviation

$$s = \sqrt{s^2}$$

- Units the same as the measurement
- If distribution is normal, 67% of data within 1 SD, 95% within 2
- σ if describing the population

Exercise: Sample Size and Estimated Sample Variation

1. Repeat the last exercise, but with the functions sd or var
2. Do you need as many samples for a precise estimate as for the mean?

Next time…